

Theory of neutron scattering as a probe of the superconducting gap in the iron pnictides

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Inelastic neutron scattering provides a probe for studying the spin and momentum structure of the superconducting gap. Here, using a two-orbital model for the Fe-pnictide superconductors and a random-phase approximation–BCS approximation for the dynamic spin susceptibility, we explore the scattering response for various gaps that have been proposed.

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I. INTRODUCTION

Recent neutron-scattering experiments have shown that LaOFeAs undergoes a structural distortion below ~ 150 K, which is then followed at ~ 137 K by the onset of long-range spin-density wave (SDW) order with a wave vector $\mathbf{q}=(0.5,0.5,0.5)\pi/a$.^{1,2} When it is doped with F, both the structural distortion and the magnetic order are suppressed and the system becomes superconducting.² When La is replaced by Sm, superconducting transition temperatures of 55 K have been reported.³ Thus it is natural to believe that the Fe-pnictide superconductors have an electronic pairing mechanism, and a variety of unconventional gap structures have already been proposed.^{4–11} Here we explore how inelastic neutron scattering in the superconducting state can provide information on which the gap structures actually occur.

Band-structure calculations for doped LaOFeAs give a Fermi surface for the 2-Fe/cell Brillouin zone, which consists of two hole cylinders around the Γ point and two-electron cylinders around the M point.^{4,6,12} Here we will work in a larger Brillouin zone, which is associated with a square lattice of Fe sites having 1-Fe/cell. In this case the SDW would be associated with $\mathbf{q}=(\pi,0)$ or $(0,\pi)$. Here we will use a simple two-orbital per site tight-binding model, which has been parametrized to give the Fermi surface shown in Fig. 1.¹³ While folding this down to the 1-Fe/cell Brillouin zone gives four Fermi surfaces in qualitative agreement with the band-structure calculations, the α_2 Fermi surface shown in Fig. 1(a) should, in fact, appear around the Γ point and reflects a limitation of the two-orbital model.^{4,8} Here the transitions that we will discuss come dominantly from the α_1 and β_1 Fermi surfaces, which are in agreement with the band-structure Fermi surfaces. We then assume that the spin susceptibility in the superconducting state can be modeled by a random-phase approximation (RPA)-BCS form and proceed to explore the structure of the inelastic scattering in the superconducting state for two \mathbf{q} values and various gaps. As one knows from the cuprate problem, the occurrence of resonances in the neutron scattering depend, through the BCS coherence factors, on the relative signs of the gap on different parts of the Fermi surface, which are separated by \mathbf{q} . For the present case, in which there are multiple Fermi surfaces, there is a variety of ways in which resonances can occur and provide information on the gap structure.

In the following, we first give a brief review of the model and then outline the RPA-BCS calculation of the spin susceptibility. This is similar to various approximations used for both the cuprates¹⁴ and Sr₂RuO₄.¹⁵ We calculate the normal RPA spin susceptibility and then examine the RPA-BCS response in the superconducting state for both singlet and triplet gap functions. A related study based on a four-band model was reported in Ref. 16 for the case of a singlet gap. However, these authors neglected to take into account the matrix elements, which relate the band operators to the orbital operators. The singlet gap functions we will use correspond to low-order lattice harmonic representations of the sign-reversed s -wave gap proposed by Mazin *et al.*,⁴

$$\Delta_{s^*}(\mathbf{k}) = \Delta_0 \cos k_x \cos k_y, \quad (1)$$

and an extended s -wave gap,

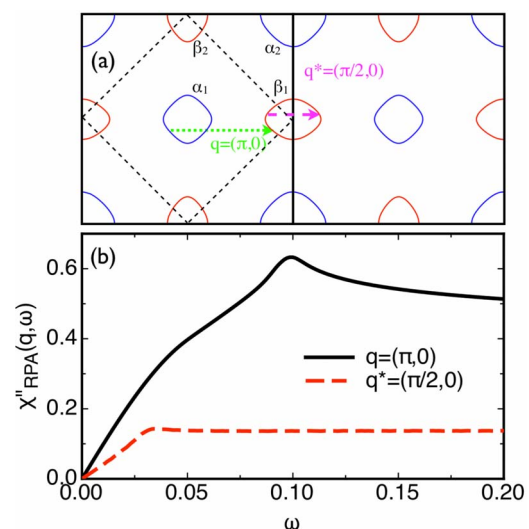


FIG. 1. (Color online) (a) Fermi surface of the two-orbital model in the large 1-Fe/cell Brillouin zone. The $\alpha_{1/2}$ Fermi-surface sheets are hole pockets given by $E_-(\mathbf{k}_F)=0$, and the $\beta_{1/2}$ sheets are electron pockets given by $E_+(\mathbf{k}_F)=0$. The nesting vectors $\mathbf{q}=(\pi,0)$ and $\mathbf{q}^*=(\pi/2,0)$ are indicated by the dotted and dashed lines, respectively. (b) RPA spin susceptibility $\chi''_{\text{RPA}}(\mathbf{q},\omega)$ versus frequency in the normal state [$\Delta(\mathbf{k})=0$] for $\mathbf{q}=(\pi,0)$ and $\mathbf{q}^*=(\pi/2,0)$.

$$\Delta_{xs}(\mathbf{k}) = \frac{\Delta_0}{2} (\cos k_x + \cos k_y). \quad (2)$$

We will also determine the spin-flip $\chi''_{+-}(\mathbf{q}, \omega)$ and non-spin-flip $\chi''_{zz}(\mathbf{q}, \omega)$ responses for various p -wave triplets. In this case,

$$\Delta_{\alpha\beta}(\mathbf{k}) = [\vec{d}(\mathbf{k}) \cdot \vec{\sigma} i \sigma_2]_{\alpha\beta}, \quad (3)$$

with \vec{d} perpendicular to the Fe plane and $d_z(\mathbf{k}) = \Delta(\mathbf{k})$. Here we will explore $\Delta(\mathbf{k}) = \sin k_x$, $\sin 2k_x$, and $\sin k_x + i \sin k_y$. We conclude with a summary of what one can expect to learn about the gap symmetry from inelastic neutron scattering in the superconducting state.

II. MODEL

Band-structure calculations for doped LaOFeAs show that the low-energy states near the Fermi energy have dominant $3d$ Fe character and various multi-orbital tight-binding fits have been proposed. Here we will use a minimal two-orbital d_{xz} - d_{yz} per site tight-binding model with parameters chosen to give the Fermi surfaces shown in Fig. 1(a). This model has the virtue of simplicity while qualitatively capturing the shapes of the relevant band-structure Fermi surfaces. This latter feature is important since it is the variation of the gaps on the Fermi surfaces that determine, through the BCS coherence factors, the inelastic neutron-scattering response. While the magnitude of the response depends on the Fermi velocities on the Fermi surfaces, which are not well reproduced by the two-orbital model, the occurrence or nonoccurrence of resonant features is determined by the k dependence of the gap and the existence of multiple Fermi surfaces.

As described in Ref. 13, our minimal model consists of a square two-dimensional lattice with degenerate d_{xz} and d_{yz} orbitals on each site. One-electron hopping parameters t_i are introduced, which provide near-neighbor $\sigma(t_1)$ and $\pi(t_2)$ couplings between similar orbitals, as well as a next-nearest-neighbor coupling t_3 . In addition, there is a next-nearest-neighbor coupling t_4 , which hybridizes d_{xz} with d_{yz} . The resulting tight-binding Hamiltonian can be written as

$$H_0 = \sum_{\mathbf{k}\sigma} \psi_{\sigma}^{\dagger}(\mathbf{k}) [(\varepsilon_{+}(\mathbf{k}) - \mu)\mathbb{I} + \varepsilon_{-}(\mathbf{k})\tau_3 + \varepsilon_{xy}(\mathbf{k})\tau_1] \psi_{\sigma}, \quad (4)$$

with

$$\psi_{\sigma}(\mathbf{k}) = \begin{pmatrix} d_{x\sigma}(\mathbf{k}) \\ d_{y\sigma}(\mathbf{k}) \end{pmatrix}. \quad (5)$$

Here τ_i are the usual Pauli matrices, and

$$\varepsilon_{\pm}(\mathbf{k}) = \frac{1}{2} [\varepsilon_x(\mathbf{k}) \pm \varepsilon_y(\mathbf{k})],$$

$$\varepsilon_x(\mathbf{k}) = -2t_1 \cos k_x - 2t_2 \cos k_y - 4t_3 \cos k_x \cos k_y,$$

$$\varepsilon_y(\mathbf{k}) = -2t_2 \cos k_x - 2t_1 \cos k_y - 4t_3 \cos k_x \cos k_y,$$

$$\varepsilon_{xy}(\mathbf{k}) = -4t_4 \sin k_x \sin k_y. \quad (6)$$

Introducing the band operator $\gamma_{\nu\sigma}(\mathbf{k})$, such that for $r=x$ or y

$$\psi_{r\sigma}(\mathbf{k}) = \sum_{\nu=\pm} a_r^{\nu}(\mathbf{k}) \gamma_{\nu\sigma}(\mathbf{k}), \quad (7)$$

with

$$a_{+}^x(\mathbf{k}) = a_{-}^y(\mathbf{k}) = \text{sgn}[\varepsilon_{xy}(\mathbf{k})] \sqrt{\frac{1}{2} + \frac{\varepsilon_{-}(\mathbf{k})}{2\sqrt{\varepsilon_{-}^2(\mathbf{k}) + \varepsilon_{xy}^2(\mathbf{k})}}},$$

$$a_{+}^y(\mathbf{k}) = -a_{-}^x(\mathbf{k}) = \sqrt{\frac{1}{2} - \frac{\varepsilon_{-}(\mathbf{k})}{2\sqrt{\varepsilon_{-}^2(\mathbf{k}) + \varepsilon_{xy}^2(\mathbf{k})}}}, \quad (8)$$

the tight-binding Hamiltonian becomes

$$H_0 = \sum_{\nu=\pm, \sigma} E_{\nu}(\mathbf{k}) \gamma_{\nu\sigma}^{\dagger}(\mathbf{k}) \gamma_{\nu\sigma}(\mathbf{k}). \quad (9)$$

Here the band energies are

$$E_{\pm}(\mathbf{k}) = \varepsilon_{\pm}(\mathbf{k}) \pm \sqrt{\varepsilon_{-}^2(\mathbf{k}) + \varepsilon_{xy}^2(\mathbf{k})} - \mu. \quad (10)$$

We choose the hopping parameters $t_1 = -1$, $t_2 = 1.3$, and $t_3 = t_4 = -0.85$ and chemical potential $\mu = 1.45$. The α_1 and α_2 Fermi surfaces in Fig. 1(a) correspond to $E_{-}(\mathbf{k}_F) = 0$, while the β_1 and β_2 surfaces are given by $E_{+}(\mathbf{k}_F) = 0$.

III. INELASTIC NEUTRON SCATTERING

The physical spin susceptibility

$$\chi_{ij}(q, i\omega_m) = \sum_{r,t} \chi_{ij}^{rrtt}(\mathbf{q}, i\omega_m) \quad (11)$$

is calculated from the orbital-dependent spin susceptibility defined as

$$\chi_{ij}^{rstu}(\mathbf{q}, i\omega_m) = \int_0^{\beta} d\tau e^{i\omega_m \tau} \langle T_{\tau} S_i^{rs}(\mathbf{q}, \tau) S_j^{tu}(-\mathbf{q}, 0) \rangle. \quad (12)$$

Here, $r, s = x, y$ label the orbital indices, and $S_i^{rs}(\mathbf{q}) = \frac{1}{2} \sum_{\mathbf{k}} \psi_{r\alpha}^{\dagger}(\mathbf{k} + \mathbf{q}) \sigma_{\alpha\beta}^j \psi_{s\beta}(\mathbf{k})$ is the i th component of a generalized spin operator acting between orbitals r and s . In the BCS framework, one obtains for the BCS orbital-dependent spin susceptibility,

$$\chi_{ij,0}^{rstu}(\mathbf{q}, \omega_m) = -\frac{1}{2} \sigma_{\alpha\beta}^i \sigma_{\gamma\delta}^j \sum_{\mathbf{k}, n} M_{rstu}^{\nu\nu'}(\mathbf{k}, \mathbf{q})$$

$$\times \{G_{\delta\alpha}^{\nu}(k+q) G_{\beta\gamma}^{\nu'}(k) + F_{\alpha\gamma}^{\dagger\nu}(-k-q) F_{\beta\delta}^{\nu'}(k)\}. \quad (13)$$

Here we used $k = (\mathbf{k}, \omega_n)$ and $q = (\mathbf{q}, \omega_m)$ and $\nu, \nu' = +, -$ are the eigenvalues of the bands. The normal and anomalous Green's functions for band ν are given by

$$G_{\alpha\beta}^{\nu}(\mathbf{k}) = -\delta_{\alpha\beta} \frac{i\omega_m + E_{\nu}(\mathbf{k})}{\omega_m^2 + \mathcal{E}_{\nu}^2(\mathbf{k})}, \quad F_{\alpha\beta}^{\nu}(\mathbf{k}) = \frac{\Delta_{\alpha\beta}(\mathbf{k})}{\omega_m^2 + \mathcal{E}_{\nu}^2(\mathbf{k})}, \quad (14)$$

with $\mathcal{E}_{\nu}(\mathbf{k}) = \sqrt{E_{\nu}^2(\mathbf{k}) + |\Delta(\mathbf{k})|^2}$. The hybridization between the bands is reflected in the matrix elements

$$M_{rstu}^{vv'}(\mathbf{k}, \mathbf{q}) = a_{rv}^r(\mathbf{k} + \mathbf{q}) a_{vt}^s(\mathbf{k}) a_{rt}^t(\mathbf{k}) a_{su}^u(\mathbf{k} + \mathbf{q}). \quad (15)$$

Although these matrix elements change when more orbitals are included, we find qualitatively similar results for the resonance in preliminary studies of a four-orbital model.

One can then obtain the BCS spin susceptibility $\chi_{ij,0}(\mathbf{q}, \omega) = \sum_{r,t} \chi_{ij,0}^{rrtt}(\mathbf{q}, \omega)$ on the real frequency axis from an analytical continuation of Eq. (13). We then use the RPA to take into account the effect of the on-site intraorbital and interorbital Coulomb interactions U and U' , respectively.¹¹ The RPA susceptibility is determined from the matrix equation

$$\chi_{ij,\text{RPA}}(q) = \sum_{r,t} \{ \chi_{ij,0}(q) [\mathbb{1} - \Gamma \chi_{ij,0}(q)]^{-1} \}_{rr,tt}, \quad (16)$$

where $q = (\mathbf{q}, \omega)$ with the interaction vertex $\Gamma = U \mathbb{1}_{4 \times 4}$. Here we have set $U' = U$, and for a given q , $\chi_0^{ij}(q)$ is a 4×4 matrix in the basis $(rs) = (xx, xy, yx, yy)$.

Figure 1(b) shows the results for the imaginary part of the RPA spin susceptibility $\chi_{\text{RPA}}''(\mathbf{q}, \omega)$ in the normal state ($\Delta_0 = 0$) for $\mathbf{q} = (\pi, 0)$ and $\mathbf{q}^* = (\pi/2, 0)$. Here we used $U = 3|t_1|$, $\mu = 1.45$, and the temperature $T = 0.001|t_1|$. For $\mu = 1.45$, the static RPA spin susceptibility shows peaks at $\mathbf{q} = (\pi, 0)$ and $\mathbf{q}^* = (\pi/2, 0)$.¹³ As indicated by the dotted and dashed arrows in Fig. 1(a), $\mathbf{q} = (\pi, 0)$ is a nesting vector between regions on the α_1 and β_1 Fermi-surface sheets. The scattering for $\mathbf{q}^* = (\pi/2, 0)$ is dominated by the intraband excitations on the β_1 Fermi surface sheet [see Fig. 1(a)] since for other interband processes with $\mathbf{q} = (\pi, 0)$, $\varepsilon_{xy}(\mathbf{k})$ and $\varepsilon_{xy}(\mathbf{k} + \mathbf{q}^*)$ are close to zero, and therefore the matrix elements $M_{rrtt}^{vv'}(\mathbf{k}, \mathbf{q})$ are very small. At low frequency $\chi_{\text{RPA}}''(\mathbf{q}, \omega)$ is larger for $\mathbf{q} = (\pi, 0)$ than for $\mathbf{q} = (\pi/2, 0)$ since larger regions of the Fermi surface are nested. At low frequency the RPA susceptibility is strongly enhanced over the unrenormalized susceptibility (not shown).

In the superconducting state, the gap $\Delta(\mathbf{k})$ is finite and the susceptibility, Eq. (13), depends on the symmetry of the gap. For singlet pairing one has $F_{\uparrow\downarrow}(\mathbf{k}) = -F_{\uparrow\downarrow}(\mathbf{k})$ and $F_{\uparrow\downarrow}(-\mathbf{k}) = F_{\uparrow\downarrow}(\mathbf{k})$ and hence the in-plane susceptibility $\chi_{+-} = \frac{1}{2}(\chi_{xx} + \chi_{yy})$ is equal to the out-of-plane susceptibility χ_{zz} as in the normal state. For the triplet case, however, one has $F_{\uparrow\downarrow}(\mathbf{k}) = F_{\uparrow\downarrow}(\mathbf{k})$ and $F_{\uparrow\downarrow}(-\mathbf{k}) = -F_{\uparrow\downarrow}(\mathbf{k})$. Therefore χ_{+-} and χ_{zz} differ with respect to their superconducting coherence factors.

IV. RESULTS

As is well known, the BCS coherence factors that enter the spin susceptibility depend upon the sign of $\Delta(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k})$. For a singlet gap, when this is negative, there can be a resonance response at $\omega = |\Delta(\mathbf{k} + \mathbf{q})| + |\Delta(\mathbf{k})|$. For a triplet gap, the coherence factors are different for χ_{zz} and χ_{+-} . In this case, when $\text{Re}[\Delta^*(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k})]$ is negative, there can be a resonance in χ_{zz}'' but not in χ_{+-}'' . Likewise, when $\text{Re}[\Delta^*(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k})]$ is positive, χ_{+-}'' can exhibit a resonance while χ_{zz}'' varies smoothly through $\omega = |\Delta(\mathbf{k} + \mathbf{q})| + |\Delta(\mathbf{k})|$. Thus, the neutron-scattering response in the superconducting state can provide information on the momentum and spin

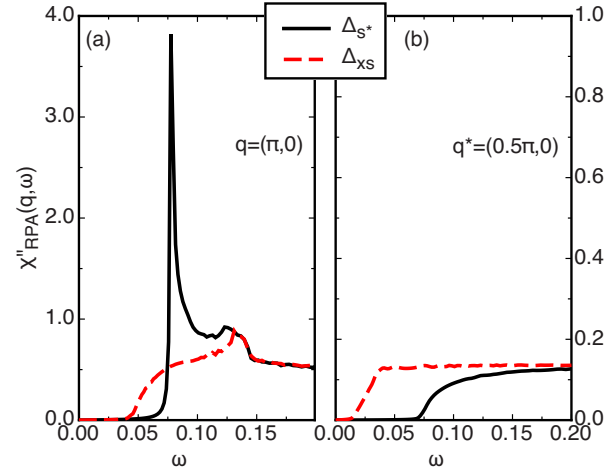


FIG. 2. (Color online) RPA dynamic spin susceptibility $\chi_{\text{RPA}}''(\mathbf{q}, \omega)$ versus frequency in the spin singlet superconducting state for the sign-reversed s -wave gap (solid line) and the extended s -wave gap (dashed line) for (a) $\mathbf{q} = (\pi, 0)$ and (b) $\mathbf{q}^* = (\pi/2, 0)$.

structure of the superconducting gap. Here we examine the response for various gaps that have been proposed for LaOFeAs.

To begin, Fig. 2(a) shows the imaginary part of the RPA-BCS spin susceptibility for two different singlet gaps at a momentum transfer $\mathbf{q} = (\pi, 0)$. Here we have set $\Delta_0 = 0.05$. We have modeled a sign-reversed s -wave gap $\Delta_{s^*}(\mathbf{k})$; i.e., the type proposed by Mazin *et al.*⁴ by Eq. (1) and the solid line in Fig. 2(a) shows the expected resonance response associated with having $\Delta(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k}) < 0$. This behavior can be contrasted with the response found for an extended s -wave gap. Here $\Delta(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k}) > 0$ for the $\mathbf{q} = (\pi, 0)$ nesting vector.

Figure 2(b) shows the results for $\mathbf{q}^* = (\pi/2, 0)$. For this momentum transfer the scattering is dominated by the intraband process connecting regions on the β_1 Fermi-surface sheet. For these regions one has $\mathbf{k} + \mathbf{q}^* = -\mathbf{k}$, and therefore $\Delta(\mathbf{k} + \mathbf{q}^*)\Delta(\mathbf{k}) > 0$ for the singlet gaps. Thus, no resonance is found for $\mathbf{q}^* = (\pi/2, 0)$ in this case.

Similar results for various triplet gaps are shown in Fig. 3 for $\mathbf{q} = (\pi, 0)$. For the p_x -wave $\sin k_x$ gap, $\Delta(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k}) < 0$, and a resonance is seen in $\chi_{zz}''(\mathbf{q}, \omega)$ but not in $\chi_{+-}''(\mathbf{q}, \omega)$. One could also consider a sign-reversed p wave modeled by $\Delta_{p2x} = \Delta_0 \sin 2k_x$. Here the coherence factor for $\mathbf{q} = (\pi, 0)$ is positive so that the resonance appears in $\chi_{+-}''(\mathbf{q}, \omega)$. For the $\sin k_x + i \sin k_y$ gap, $\sin k_x \sin(k_x + q_x) < 0$ and $\sin k_y \sin(k_y + q_y) > 0$ with similar size for the dominant process. Hence, $\text{Re}[\Delta^*(\mathbf{k} + \mathbf{q})\Delta(\mathbf{k})]$ is close to zero, and one obtains qualitatively similar results for χ_{+-}'' and χ_{zz}'' .

Figure 4 shows the results for the triplet gaps for $\mathbf{q}^* = (\pi/2, 0)$. For the p_x -wave $\sin k_x$ gap, the results are similar as in Fig. 3 for $\mathbf{q} = (\pi, 0)$. The gap changes sign under the transformation $\mathbf{k} \rightarrow -\mathbf{k}$ so that the gap has opposite signs on the sheets of the β_1 Fermi pocket connected by \mathbf{q}^* [see Fig. 1(a)]. Hence, $\chi_{zz}''(\mathbf{q}, \omega)$ displays a resonance while $\chi_{+-}''(\mathbf{q}, \omega)$ does not. For the $\sin 2k_x$ gap, the situation is similar, and a resonance is found in χ_{zz}'' but not in χ_{+-}'' . This is opposite to the results in Fig. 3 for $\mathbf{q} = (\pi, 0)$. The results for the $\sin k_x + i \sin k_y$ case are almost identical to the results

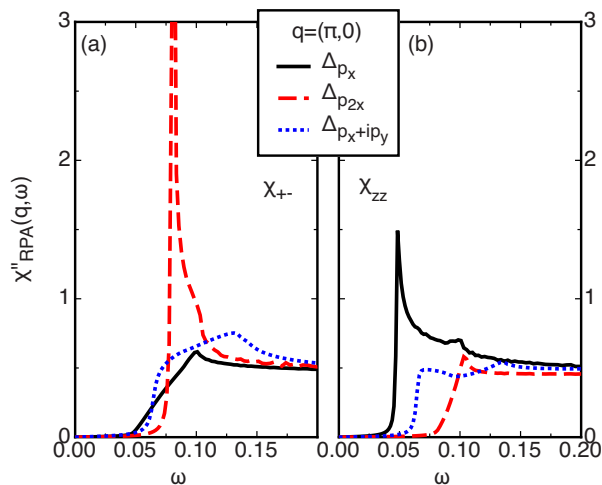


FIG. 3. (Color online) RPA spin susceptibility (a) $\chi''_{+-}(\mathbf{q}, \omega)$ and (b) $\chi''_{zz}(\mathbf{q}, \omega)$ versus frequency for $\mathbf{q}=(\pi, 0)$ in the spin triplet superconducting state for a p_x -wave gap (solid line), a sign-reversed p -wave gap (dashed line), and a p_x+ip_y -wave gap (dotted line).

found for the p_x -wave gap. This is explained by the fact that for the dominant intraband scattering on the β_1 Fermi-surface sheet, \mathbf{k}_y and $\mathbf{k}_y + \mathbf{q}_y$ are close to zero, and therefore the $\sin k_y$ contribution to the p_x+ip_y gap is an order of magnitude smaller than the $\sin k_x$ contribution.

V. CONCLUSION

Using a two-orbital model for the Fe-pnictide superconductors and an RPA-BCS approximation for the dynamic spin susceptibility we have explored the inelastic-scattering response for various singlet and triplet gaps that have been proposed. As one would expect, we have found that the occurrence of resonances in the dynamic spin susceptibility $\chi''(\mathbf{q}, \omega)$ depends on the relative signs of the gap on the parts of the Fermi surface separated by \mathbf{q} , and in the case of triplet gaps also on whether the in-plane, χ''_{+-} , or out-of-plane, χ''_{zz} ,

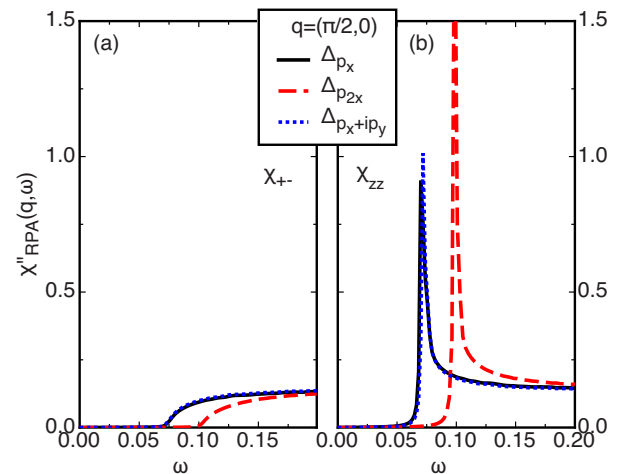


FIG. 4. (Color online) RPA spin susceptibility (a) $\chi''_{+-}(\mathbf{q}, \omega)$ and (b) $\chi''_{zz}(\mathbf{q}, \omega)$ versus frequency for $\mathbf{q}^*=(\pi/2, 0)$ in the spin triplet superconducting state for a p_x -wave gap (solid line), a sign-reversed p -wave gap (dashed line), and a p_x+ip_y -wave gap (dotted line).

components are studied. Specifically, for the singlet gaps, we have found that $\chi''(\mathbf{q}, \omega)$ displays a resonance for a sign-reversed s -wave gap modeled by $\Delta_0 \cos k_x \cos k_y$ for $\mathbf{q}=(\pi, 0)$, which corresponds to the antiferromagnetic wave vector but no resonance for the extended s -wave gap or for $\mathbf{q}^*=(\pi/2, 0)$. For the triplet case, resonances were found for a p_x -wave gap in $\chi''_{zz}(\mathbf{q}, \omega)$ and for a sign-reversed p -wave gap in $\chi''_{+-}(\mathbf{q}, \omega)$ for $\mathbf{q}=(\pi, 0)$. For $\mathbf{q}^*=(\pi/2, 0)$, resonances appeared in $\chi''_{zz}(\mathbf{q}, \omega)$ for the p wave, sign-reversed p wave, and p_x+ip_y -wave gaps.

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